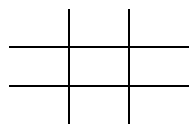
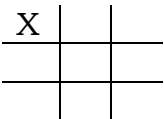


First move

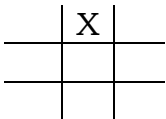


X's turn

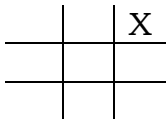
can lead to any one of



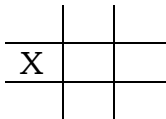
a1



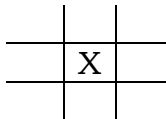
a2



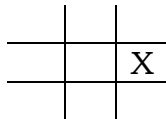
a3



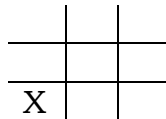
a4



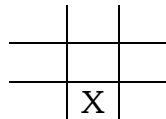
a5



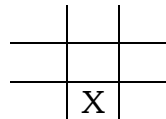
a6



a7



a8

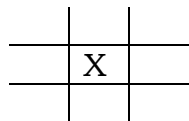


a9

O's  
turn

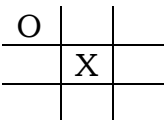
Just looking at a5:

Second move

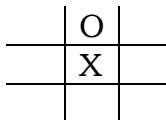


O's turn

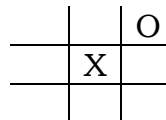
can lead to any one of



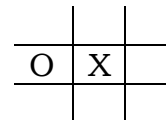
b1



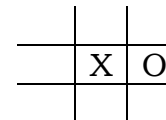
b2



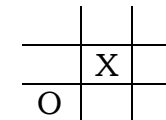
b3



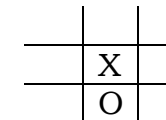
b4



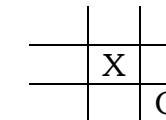
b5



b6



b7



b8

X's turn

Just looking at b3:

Third move

		O
	X	

X's turn

can lead to any one of

X		O
	X	

c1

	X	O
	X	

c2

		O
X	X	

c3

		O
	X	X

c4

		O
	X	
X		

c5

		O
	X	
	X	

c6

		O
	X	
		X

c7

O's turn

Just looking at c6:

Fourth move

		O
	X	
	X	

O's turn

can lead to any one of

O		O
	X	
	X	

d1

	O	O
	X	
	X	

d2

		O
O	X	
	X	

d3

		O
	X	O
	X	

d4

		O
	X	
O	X	

d5

		O
	X	
	X	O

d6

X's turn

Just looking at d3:

Fifth move

		O
O	X	
	X	

X's turn

can lead to any one of

X		O
O	X	
	X	

e1

	X	O
O	X	
	X	

e2

		O
O	X	X
	X	

e3

		O
O	X	
X	X	

e4

		O
O	X	
	X	X

e5

But as this is X's turn, X would obviously pick 2 and the game would be over.  
X and O can both look ahead in the same way.  
Seeing this outcome, O would not have picked d3 for the fourth move.  
O would have picked a d<sub>i</sub> that leads to O winning (if there was one)

But knowing that, X would not have picked c6 for the third move.  
How would anyone ever pick any move?

## Minimax search

`new_board(N)` is [ [' ' ] \* N for i in range(0, N) ]

`possible_moves(board)` is list of int pairs (row, col) of all empty spaces

`move(board, whose_turn, (row, col))`

    whose\_turn is 'X' or 'O'

    just creates new board same as old with that one extra move made

`ended(board)` = bool, no more moves possible: either someone has won or no blank squares left

`utility(board, player)` = int, score for that board from player's point of view, assuming the game is over  
    +1 for win, 0 for tie, -1 for loss.

```
def minimax_strategy(board, perspective, whose_turn, other_player):
    if ended(board):
        score = utility(board, whose_turn)
    elif perspective == whose_turn:
        best = -2
        for rowcol in possible_moves(board):
            new_board = move(board, whose_turn, rowcol)
            score = minimax_strategy(new_board, perspective, other_player, whose_turn)
            if score > best:
                best = score
                the_move = rowcol
    else:
        worst = +2
        for rowcol in possible_moves(board):
            new_board = move(board, whose_turn, rowcol)
            score = minimax_strategy(new_board, perspective, other_player, whose_turn)
            if score < worst:
                worst = score
                the_move = rowcol
    return score      # Naturally we would want to return the_move too, this is just keeping it simple.
```